Department of Mathematics University of Notre Dame Math 10120 – Finite Math Fall 2020

Name:\_\_\_\_\_

Instructor: Jacob Landgraf

# Exam 1

### September 2, 2020

This exam is in two parts on 8 pages and contains 12 problems worth a total of 100 points. You have 1 hour and 30 minutes to work on it. You may use a calculator, but no books, notes, or other aid is allowed. Be sure to write your name on this title page and put your initials at the top of every page in case pages become detached.

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Place an  $\times$  through your answer to each problem.

1.	(a)	(b)	(c)	(d)	(e)
2.	(a)	(b)	(c)	(d)	(e)
3.	(a)	(b)	(c)	(d)	(e)
4.	(a)	(b)	(c)	(d)	(e)
5.	(a)	(b)	(c)	(d)	(e)
6.	(a)	(b)	(c)	(d)	(e)
7.	(a)	(b)	(c)	(d)	(e)
8.	(a)	(b)	(c)	(d)	(e)

MC. \_\_\_\_\_\_ 9. \_\_\_\_\_ 10. \_\_\_\_\_ 11. \_\_\_\_\_ 12. \_\_\_\_\_ Tot. \_\_\_\_\_

## **Multiple Choice**



**1.** (5 pts.) In the following Venn diagram, which of the following is equal to  $B' \cup (C \cap A')$ ? (Note the "prime" over the A and the B.)

All clubs: C(13,4)

diamonds: C(13,4)

**3.** (5 pts.) Claire has 4 mystery novels and Emily has 8 mystery novels (all different). They decide to go on a vacation together, and agree to bring two mystery novels each. In how many ways can they choose which 4 books they will take? (Note that the only issue is **which** two books each chooses, not what order they choose them.)



**4.** (5 pts.) A standard deck consists of 52 cards, with 13 cards in each of four suits (clubs, diamonds, hearts and spades). So there are four A's, four 2's, four 3's, etc. A "hand" is a subset of four cards. How many hands are **not** all of the same suit?

- (a)  $4 \cdot P(13, 4)$
- (c)  $C(13,1)^4$
- (e) C(52,4) C(13,4)

hearts : C(13,4) # hends w ands wi spectes : ((13,4)+ all same suit all some hands Suit 4. C(13,4)  $= ((52,4) - 4 \cdot C(13,4))$ 

(b)  $C(52,4) - 4 \cdot P(13,4)$ 

(d)  $C(52, 4) - 4 \cdot C(13, 4)$ 

**5.** (5 pts.) Mr. Chips is making up a true-false quiz for his class. He wants to put 9 questions in the quiz. In how many ways can he arrange it so that four of the answers are True and five are False?



**6.** (5 pts.) The following grid is part of a street map of a city. Javier starts at point A and wants to get to point C going only to the right and down (on the map). However, along the way he wants to visit his brother Rafi, who is at point B. How many routes from A to C pass by B?



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Initials:\_\_\_\_

7. (5 pts.) The Aviation Club has 9 members. An anonymous donor offers them a free trip on a hot air balloon, but there are two conditions: At least one member of the club has to go (since someone has to control the balloon), and and most 7 can go (because of the capacity of the balloon). In how many way can they decide who goes on the trip?



8. (5 pts.) Mary is planning to give Dave 32 DVD's for Christmas. Since that's a bit bulky, she decides to divide them into four groups of 8 to giftwrap. (Note that the order of these four groups is irrelevant.) In how many ways can she choose to divide them up?



#### **Partial Credit**

You must show all of your work on the partial credit problems to receive credit! <u>Make sure that your answer is in the answer box</u>. You're more likely to get partial credit for a wrong answer if you explain your reasoning.

**9.** (15 pts.) A PIN number for a bank account consists of 5 digits (e.g. 29010). Your answers in this problem do not have to be numbers. You can use P(n,r), C(n,r), exponents or factorials.

(a) How many PIN numbers are there if you are allowed to repeat digits?



(b) How many PIN numbers are there if you are not allowed to repeat digits?



Answer to (b): 
$$P(10,5)$$

(c) How many PIN numbers have at least one repeated digit? [Hint: Think about what you did in the first two parts.]

**#PINS** w' = **# total** = **#PINS**  $w' = 10^{5} - P(10,5)$  **>| repect** PINS no repeats Answer to (c):  $10^{5} - P(10,5)$ 

10. (15 pts.) A group of 190 people decided to check ancestry.com for the preceding five generations to see what nationalities they found (not necessarily just one). Here is the relevant data:

- 45 have **ONLY** Italian ancestry (I).
- 15 have **ONLY** British ancestry (B).
- 30 have **ONLY** German ancestry (G).
- 20 have Italian and British ancestry but **NOT** German.
- 40 have British and German ancestry but **NOT** Italian.
- 5 have Italian and German ancestry but **NOT** British.
- 25 do **NOT** have any of the three ancestries.

Fill in **all** regions of the following Venn diagram.



11. (15 pts.) In this problem you will be looking at the word

ADDITIONALLY.

There are two A's, two D's, two I's, one T, one O, one N, two L's, and one Y, for a total of 12 letters. For each part of the problem, be sure to explain your work and give a numerical answer.

(a) How many **different** 12-letter "words" can be made from these letters?



(b) How many different 5-letter "words" can be made from these letters if we insist that each word consist of different letters? [Hint: how many different letters are there?]

different letters, want 5 of them (in order)  $\sim P(9,5) = 9.8.7.6.5$ 

Answer to (b): Remember this has to be a number! 15,120

12. (15 pts.) A bag contains 18 colored marbles, of which 6 are red, 5 are white, 4 are blue and 3 are orange. (Assume that marbles of the same color are distinguishable from each other. In this problem, the order that you pick the marbles does not matter.) I plan to pick 3 marbles from the bag.

**Note:** In the following two parts, it is not necessary to give a numerical answer, i.e. you may express your answers using the notation for permutations (P(n, k)), combinations (C(n, k)), factorials (n!) and powers  $(a^k)$ .

(a) In how many total ways can I choose the three marbles if I don't care about the colors?



(b) In how many ways can I pick the three marbles so that they are all different colors?

7 RWB: 6.5.4 = 120 ways -> RW D: 6.5.3 = 90 w~ -> RB D: 6.4.3 = 72 wys WBO: 5-4-3=60~~ Answer to (b): 242

(c) In how many ways can I pick the three marbles so that they are all the same color?

All red: ((6,3) = 20 ~ white: C(5,3) = 10 ways blue: C(4,3) = 4 ways orange: C(3,3) = Answer to (c):

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4.	(a)	(b)	(c)	$(\mathbf{q})$	(e)
5.	(a)	( <b>b</b> )	(c)	(d)	(e)
6.	(a)	(b)	(c)	(d)	$(\bullet)$
7.	(a)	(b)	(c)	$(\mathbf{q})$	(e)
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